

The spatiotemporal Ginzburg-Landau equation: dissipative solitons & stability

D. W. Bresnahan, J. M. Christian, and G. S. McDonald

Materials & Physics Research Centre, University of Salford, U.K.

Email: d.bresnahan@edu.salford.ac.uk

Keywords: dissipative solitons, Ginzburg-Landau, spatiotemporal dispersion, *energy theme*

The complex Ginzburg-Landau (GL) equation describes universal wave propagation in dispersive systems that also exhibit competition between amplification and dissipation [1,2]. The balance between dispersive effects (group-velocity dispersion and self-phase modulation), linear gain and nonlinear loss can, in principle, lead to the formation of a stationary wavepacket (or *soliton*) in the local time frame. Here, we propose a novel two-fold generalization of the traditional GL equation to accommodate additional physical effects: (i) spatiotemporal dispersion [3], and (ii) power-law nonlinearity [4]. Exact analytical bright solitons of the new model have been derived, with asymptotic analysis demonstrating the emergence of well-known solutions [1,2] in a simultaneous multiple limit. Extensive simulations have revealed that, like its conventional counterpart (see Fig. 1), the new class of spatiotemporal dissipative soliton is also susceptible to a blow-up phenomenon (where the zero-amplitude continuous-wave solution is modulationally unstable against background fluctuations of arbitrarily-small magnitude). However, a route to stabilization may be possible by coupling the soliton to a non-dispersing linear wave [5].

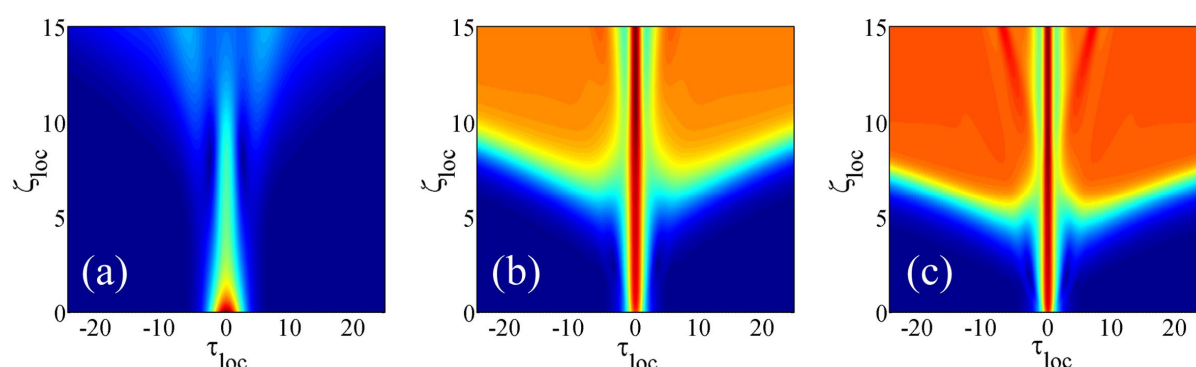


Figure 1. Instability in the conventional complex GL equation in the local time frame $(\tau_{loc}, \zeta_{loc})$ [2] for increasing strength of power-law nonlinearity. The perturbed initial-value problem corresponds to launching an input pulse whose peak intensity is lower than that predicted by the stationary solution for (a) sub-Kerr, (b) Kerr, and (c) super-Kerr systems.

References

- [1] N. R. Pereira and L. Stenflo, *Phys. Fluids* **20**, 1733 (1977).
- [2] C. Paré, L. Gagnon, and P. Bélanger, *Opt. Commun.* **74**, 228 (1989).
- [3] J. M. Christian, G. S. McDonald, T. F. Hodgkinson, and P. Chamorro-Posada, *Phys. Rev. Lett.* **108**, 034101 (2012).
- [4] J. M. Christian, G. S. McDonald, R. J. Potton, and P. Chamorro-Posada, *Phys. Rev. A* **76**, 033834 (2007).
- [5] N. Efremidis *et al.*, *Phys. Scr.* **T84**, 18 (2000).